Why optimize your code

- Computer time is a limited resource. Time on XSEDE systems is free**, but awarded on a competitive basis – very few big users get everything they want. Time on Amazon Web Services or other cloud providers costs real dollars. Maintaining your own cluster/workstation requires both time and money***.
- Optimizing your code will reduce the time to solution. Challenging problems become doable. Routine calculations can be done quickly enough to allow time for exploration and experimentation. In short, you can get more science done in the same amount of time.
- Even if computer time was free, running a computation still consumes energy. There's a lot of controversy over how much energy is used by computers and data centers, but estimates are in the 2-10% range and growing.

** XSEDE resources are not really free since someone has to pay. The NSF directly, tax payers indirectly. Average US citizen paid about \$0.07 to deploy and operate Gordon over it's lifetime

*** Of course, time *is* money when you consider opportunity costs





... but I have a parallel code and processors are getting faster, cheaper and more energy efficient

- There will always be a more challenging problem that you want to solve in a timely manner
 - Higher resolution (finer grid size, shorter time step)
 - Larger systems (more atoms, molecules, particles ...)
 - More accurate physics
 - Longer simulations
 - More replicates, bigger ensembles, better statistics
- Most parallel applications have a limited scalability
- Until we have some Earth shattering breakthroughs, there will always be limitations on availability of computation and energy consumption will be an important consideration





Guidelines for software optimization

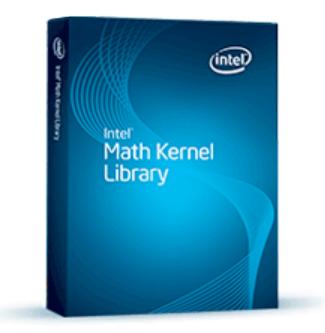
The prime directive of software optimization: **Don't break anything!** Getting correct results slowly is much better than getting wrong results quickly

- Don't obfuscate your code unless you have a really good reason (e.g. kernel in a heavily used code accounts for a lot of time)
- If you do choose to write obfuscated code, clearly document your work
- Know when to start, know when to stop
- Maintain portability. If you need to include modifications that are architecture or environment specific, use preprocessor directives to isolate key code
- Profile, optimize, repeat new hotspots may emerge
- Take advantage of optimized libraries. Unless you are a world-class expert, you are not going to write a faster matrix multiply, FFT, eigenvalue solver, etc.
- Understand the capabilities and limitations of your compiler. Use compiler options (e.g. -O3, -xHost) for best performance





Intel's Math Kernel Library (MKL)



Highly optimized mathematical library. Tuned to take maximum advantage of Intel processors. This is my first choice when running on Intel hardware.

Linear algebra (including implementations of BLAS and LAPACK), eigenvalue solvers, sparse system solvers, statistical and math functions, FFTs, Poisson solvers, non-linear optimization

Many of the routines are threaded. Easy way to get shared memory parallelism for running on a single node.

Easy to use. Just build executable with -mkl flag and add the appropriate include statement to your source (e.g. mkl.h)

https://software.intel.com/en-us/mkl_11.1_ref





MKL vs. non-MKL example

- Copy the lineq_mkl.c and lineq_nomkl.c files to your home directory. The program generates a random vector and matrix of rank N, calls the linear solver DGESV (Ax=b) then reports run time.
- Compile using the following commands

icc -O3 -o lineq_mkl lineq_mkl.c -mkl

icc -O3 -o lineq_nomkl lineq_nomkl.c -L/opt/lapack/intel/lib -lblas -llapack -lm

 On a Gordon compute node, set OpenMP threads to 1, run the two programs using a variety of problem sizes and note run times. Repeat using 2, 4, 8 and 16 threads

module load lapack export OMP_NUM_THREADS=1 ./lineq_mkl 3000 ./lineq_nomkl 3000





Know when to start / stop

Knowing when to start

- Is the code used frequently/widely enough to justify the effort?
- Does the code consume a considerable amount of computer time?
- Is time to solution important?
- Will optimizing your code help you solve new sets of problems?

Knowing when to stop

- Have you reached the point of diminishing returns?
- Is most of the remaining time spent in routines beyond your control?
- Will your limited amount of brain power and/or waking hours be better spent doing your research than optimizing the code?





Know when to start / stop

Sometimes you'll need to use your judgment

- Authors of heavily used community codes in domains such as climate and weather modeling, computational chemistry and QCD should go to extreme measures to optimize performance
- Authors of lab-specific and one-off applications should stop sooner



Jackson Pollock No. 5, 1948 (done?) Leonardo da Vinci *Mona Lisa* (done!)





Reproducibility of optimized codes

- Bit-wise reproducibility means obtaining exactly the same <u>binary</u> (internal machine representation) results
- An ASCII dump (formatted output) may <u>look</u> the same but can hide differences in the floating point representation if too few significant digits are printed
- Think about whether or not you really need bit-wise reproducibility and under which conditions (compiler, hardware, processor count). Can be done, but not without tradeoffs.
- Decide how much accuracy is needed. Is it acceptable to get a result that is correct to within a specified tolerance? Consider constructing a test suite that can be used to test reproducibility.





Confirming bit-wise reproducibility

md5sum can confirm that results are exactly the same. Uses a 128-bit cryptographic hash function to generate digital fingerprint of file. Hash collisions are possible, but probability is astronomically low.

\$ Is -Ih *

-rw-r--r-- 1 sinkovit use300 6.1M May 2 08:31 fleeting_ref_AAPL_050610.csv -rw-r--r-- 1 sinkovit use300 101M May 2 08:31 msg_AAPL_050610.csv -rw-r--r-- 1 sinkovit use300 83M May 2 08:31 settled_AAPL_050610.csv

\$ md5sum *
d7dcee609d3536d072875856d1a0c253 fleeting_ref_AAPL_050610.csv
f8655644fb37eedd1c30b8e58fe79d50 msg_AAPL_050610.csv
b77eaed47a1dc94eb75efb1d2a32432d settled_AAPL_050610.csv





Note on md5sum

- The MD5 algorithm should not be used in cases where security is an issue (digital signatures or public key certificates)
- MD5 is perfectly fine for non-secure applications where tampering would not be suspected (file transfers, confirming program output)
- More secure hash functions exist (SHA-256 or SHA-512), but they'll take longer

utility	time	hash
md5sum	13.12	cbf7e312c83db7d2d27ca3f571ee0de3
sha256sum	41.27	44b2335f1d98d5b06f28e95cc46c238a6963140b4f1 83f9223b1dc46c81f5673
sha512sum	28.90	6d09ec0c4d6db9ff64a2f9633947412ece884b92680 60c6a40c8056e38c8d5ded4d3d13c8840592db9efc 3dccbce22ac5a673993f56e2f6e1af0cb57690f447e

Timings obtained on Gordon compute node (Intel E5-2670 2.6 GHz) using 6.1 GB ASCII file





Looking for differences in ASCII files

md5sum is a great way to tell if files are identical, but is useless if there are even small differences between runs. The Linux diff utility can be used instead, provides details of the differences.

\$ wc -l file1 file2 464691 file1 Files are exactly the same length (good sign) 464691 file2 \$ md5sum file1 file2 13b71bb7b8274c1657b815735046e411 file1 Ugh, different md5sums 0234c9a3dbc4b94ade7822edc3ae2f61 file2 \$ diff file1 file2 1c1 < Fri Jun 27 12:36:02 PDT 2014 Different time stamps > Fri Jun 27 12:35:46 PDT 2014 464691c464691 < Run time: 1236.78 seconds Different run times

> Run time: 1234.56 seconds





Looking for differences in ASCII files

If the <u>acceptable changes</u> (e.g. time stamps, run times, node names) between output files occur in predictable formats and or locations, we can make clever use of sed, grep, head, tail and other utilities to build more complex tests

\$ diff file1 file2
1c1
< Fri Jun 27 12:36:02 PDT 2014 First line of output
> Fri Jun 27 12:35:46 PDT 2014
464691c464691
< Run time: 1236.78 seconds Last line of output / only line containing string 'Run time'
> Run time: 1234.56 seconds
\$ sed -n '1!p' file1 | grep -v 'Run time' | md5sum

3169c7872c74b2e1593dcde1f4d7f2be -\$ sed -n '1!p' file2 | grep -v 'Run time' | md5sum 3169c7872c74b2e1593dcde1f4d7f2be -





Using diff on directories

We can use diff to recursively compare the contents of entire directories as long as the files are named identically.

-r = recursive --brief = only report whether files differ

This will work for both plain text and binary files

\$ diff -r --brief DIR1/ DIR2/ \$

no output - directory contents identical

 \$ diff -r --brief DIR1 DIR2

 Only in DIR2: file1
 Unique to DIR2

 Only in DIR1: file2
 Unique to DIR1

 Files DIR1/fleeting_ref_AAPL_050610.csv
 Files differ – no details provided

 and DIR2/fleeting_ref_AAPL_050610.csv differ





A very brief intro to sed, grep, head, tail

grep prints the lines in a file that match (or don't match) a particular pattern	sed is a powerful stream editor that (among many other capabilities) selects lines by record number
<pre>\$ grep bird file1 # Has bird line2 bird dog cat line3 fish cat bird \$ grep -v dog file1 # Not has dog line3 fish cat bird</pre>	<pre>\$ sed -n '2p' file1 # Line 2 line2 bird dog cat \$ sed -n '2!p' file1 # All but line 2 line1 dog fish cat line3 fish cat bird</pre>
head prints the top of a file	tail prints the bottom of a file
\$ head -n1 file1 # First line	\$ tail -n1 file1 # Last line
line1 dog fish cat	line3 fish cat bird
v	
\$ head -n2 file1 # First two lines	\$ tail -n2 file1 # Last two lines
Press and the Press of the second	line of the industry of the

line1 dog fish cat line2 bird dog cat line2 bird dog cat line3 fish cat bird

SD9



Reproducibility in integer/string codes

Integers and characters are represented exactly. The same program should give the same results on any system using any compiler. When working with integers, just need to be aware of a few potential gotchas when modifying your software

(1) Division results are truncated. As a consequence, some basic arithmetic identities are not integer math identities

 $(a/b) + (c/d) \neq (ad + bc)/bd$ (2/3) + (5/2) = 0 + 2 = 2 $(2 \cdot 2 + 5 \cdot 3)/(2 \cdot 3) = 19/6 = 3$

(2) Avoid modifications to order of operations that might result in overflows

 Σ (all terms) =(?) Σ (neg terms) + Σ (pos terms)



Reproducibility in floating point codes

FP operations are subject to round-off error and seemingly trivial code modifications or changes to run conditions can change the answers. If any of the following lead to **significantly different** results, you should re-examine your algorithms

(1) Arithmetic identities that are not necessarily floating point identities.

 $(a + b) + c \neq a + (b + c)$ $(a/b) + (c/d) \neq (ad + bc)/bd$ $sqrt(sqrt(a)) \neq a^{0.25}$

(2) Software parallelization, particularly involving global reduction operations (e.g. summing over elements of an array). The exact answers may depend on the number of threads and/or processes.

(3) Aggressive compiler optimization (typically -O3 and higher) may lead to code modifications that do not preserve bit-wise reproducibility

(4) Running on different processor architectures or linking different library versions





Random number generation

Many applications rely on random number generators to set the initial conditions or perform Monte Carlo simulations. If developing your own software, do yourself a big favor and provide the capability to <u>set the seed</u>.

Can make this an optional argument that overrides the default behavior. Otherwise, you'll never be sure that the modified version of the software is correct

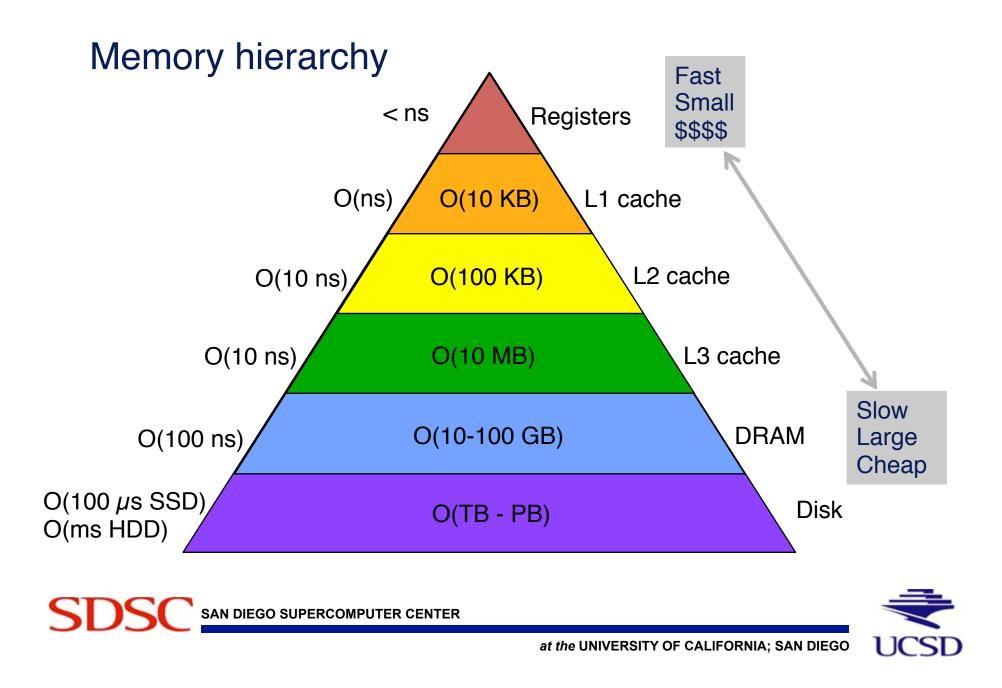
\$./a.out -i infile -o outfile ... [-seed 1234]

Seems obvious, but surprising how many code implement something like the following without documenting behavior

srandom(time(0))







Cache essentials

Temporal locality: Data that was recently accessed is likely to be used again in the near future. To take advantage of temporal locality, once data is loaded into cache, it will generally remain there until it has to be purged to make room for new data. Cache is typically managed using a variation of the Least Recently Used (LRU) algorithm.

Spatial locality: If a piece of data is accessed, it's likely that neighboring data elements in memory will be needed. To take advantage of spatial locality, cache is organized into lines (typically 64 B) and an entire line is loaded at once.

Our goal in cache level optimization is very simple – exploit the principles of temporal and spatial locality to minimize data access times





One-dimensional arrays

One-dimensional arrays are stored as blocks of contiguous data in memory.

```
int *x, n=100;
x = (int *) malloc(n * sizeof(int))
                                            relative address
                 8
                       12
                             16
                                   20
                                         24
     0
           4
                               x[4]
             x[1]
                                           x[6]
                  x[2]
                         x[3]
      x[0]
                                     x[5]
```

Cache optimization for 1D arrays is pretty straightforward and you'll probably write optimal code without even trying. Whenever possible, just access the elements in order.

```
for (int i=0; i<n; i++) {
    x[i] += 100;
}</pre>
```



One-dimensional arrays

What is our block of code doing with regards to cache?

```
for (int i=0; i<n; i++) {
    x[i] += 100;
}</pre>
```

Assuming a 64-byte cache line and 4-byte integers:

- 1. Load elements x[0] through x[15] into cache
- 2. Increment x[0] through x[15]
- 3. Load elements x[16] through x[31] into cache
- 4. Increment elements x[16] through x[31]
- 5. ...

In reality, the processor will do really clever things like recognizing the pattern of data access and **prefetching** the next cache line before it is needed.



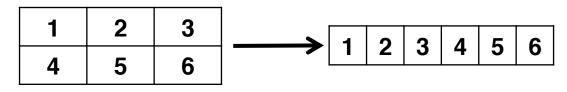


Multidimensional arrays

From the computer's point of view, there is no such thing as a twodimensional array. This is just syntactic sugar provided as a convenience to the programmer. Under the hood, array is stored as linear block of data

Column-major order: First or leftmost index varies the fastest. Used in Fortran, R, MATLAB and Octave (open-source MATLAB clone)

Row-major order: Last or rightmost index varies the fastest. Used in Python, Mathematica and C/C++







Multidimensional arrays

Properly written Fortran code

```
do j=1,n ! Note loop nesting
  do i=1,n
    z(i,j) = x(i,j) + y(i,j)
  enddo
enddo
```

Properly written C code

```
for (i=0; i<n; i++) { // Note loop nesting
  for (j=0; j<n; j++) {
    z[i][j] = x[i][j] + y[i][j]
  }
}</pre>
```



Matrix addition exercise

- Copy the dmadd_good.f and dmadd_bad.f files to your home directory. Programs perform 2D matrix addition using optimal/non-optimal loop nesting. Inspect the code and make sure you understand logic.
- Compile programs using the ifort compiler with default optimization level and explicitly stating -O0, -O1, -O2 and -O3
- On a Gordon compute node, run with matrix ranks 20,000, 30,000 and 40,000 (Programs accept single command line argument specifying the matrix rank)
- Examples: (feel free to use your own naming conventions)
 - ifort -o dmadd_good_default dmadd_good.f
 - ifort -o dmadd_bad_O3 -O3 dmadd_bad.f
 - ./dmadd_good_default 20000
 - ./dmadd_bad_O3 30000
- Keep track of the run times (reported by code)





Matrix addition exercise

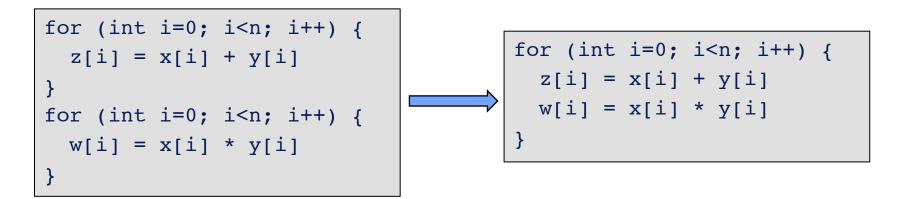
- Try to explain the timings. Under what optimization levels was there a big difference between the optimal/non-optimal versions of the codes?
- What do you think the compiler is doing?
- Why do we have that mysterious block of code after the matrix addition? What possible purpose could it serve?
- Can you make an educated guess about the default optimization level?





Loop fusion

One of the most basic loop-level optimizations is loop fusion. Two or more loops with the same range of iterations are combined into a single loop



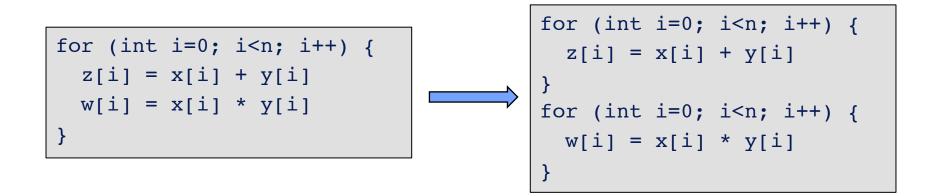
Loop fusion is hit or miss. If you really* understand computer architecture, you can probably figure out which is optimal. Need to balance cache reuse and complexity of loop body. My suggestion is to just try both and see which one is faster. Your compiler can do this automatically, but certain code features will prevent this (e.g. print statement between loops).

* By really, I mean really, really, really



Loop splitting

Loop splitting is the opposite of loop fusion. A single loop is split into two or more loops

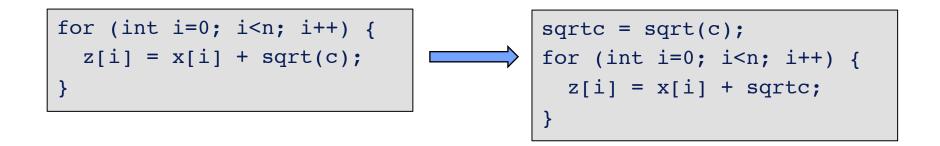


Like loop fusion, this optimization is hit or miss. Your compiler can often figure out which is optimal. Keep in mind that some loops are too complex for the compiler to analyze and you may need to manually split the loop.





Pull repeated calculation out of loop and use the pre-calculated result in its place.

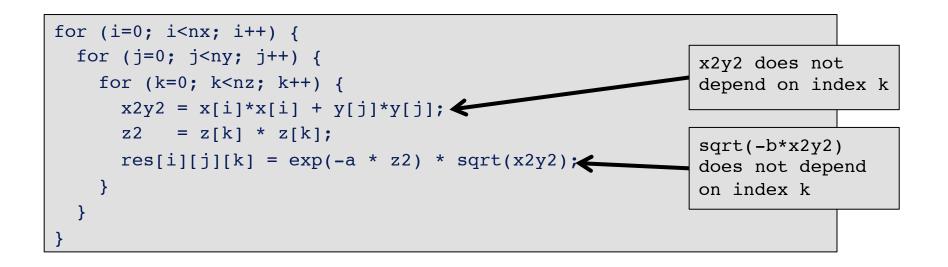


Compilers can often do this for you, particularly if the loops are simple. Still suggest that you do this yourself and be guaranteed that the optimization will be done. No real downsides.





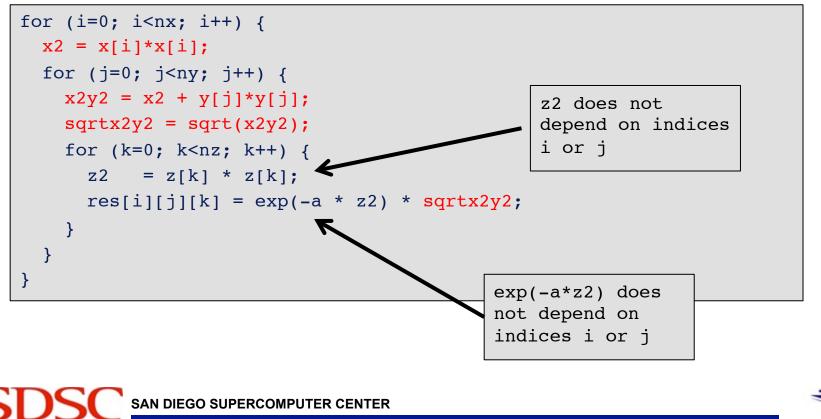
When working with nested loops, the invariants will sometime be less obvious and may even be a vector of results.







- Moved calculation of x² to outermost loop nesting Evaluated nx times instead of nx*ny*nz
- 2. Moved calculation of $sqrt(x^2+y^2)$ out one level of nesting Evaluated nx*ny times rather than nx*ny*nz



Pre-calculate vector of $exp(-a * z^2)$ results and reuse for every set of (i,j). Reduces number of exponential evaluations to nz from nx*ny*nz

```
for (k=0; k<nz; k++) {
   zterm[k] = exp(-a * z[k]*z[k]);
}
for (i=0; i<nx; i++) {
   x2 = x[i]*x[i];
   for (j=0; j<ny; j++) {
     x2y2 = x2 + y[j]*y[j];
     expx2y2 = exp(-b * x2y2);
     for (k=0; k<nz; k++) {
        res[i][j][k] = zterm[k] * sqrt2y2;
     }
   }
}</pre>
```





If out result involved $exp(-b * (x^2+y^2))$ instead of $sqrt(x^2+y^2)$, we could have taken things one step further by pre-calculating three vectors. Innermost loop would only involve multiplications

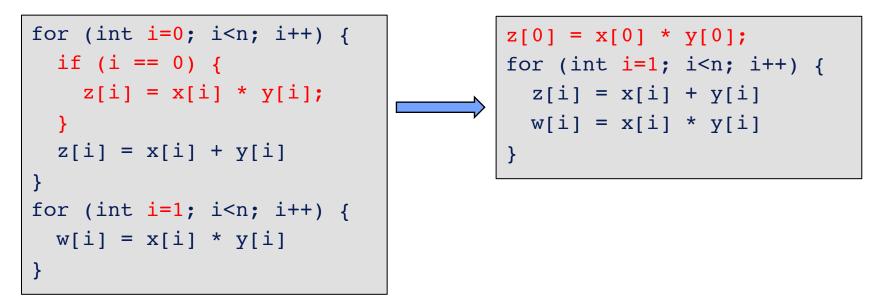
```
for (i=0; i<nx; i++) { xterm[i] = exp(-b * x[i]*x[i]); }
for (j=0; j<ny; j++) { yterm[j] = exp(-b * y[j]*y[j]); }
for (k=0; k<nz; k++) { zterm[k] = exp(-a * z[k]*z[k]); }

for (i=0; i<nx; i++) {
   for (j=0; j<ny; j++) {
     for (k=0; k<nz; k++) {
      res[i][j][k] = xterm[i] * yterm[j] * zterm[k];
     }
  }
}</pre>
```



Loop peeling

In a loop peeling optimization, one or more iterations are pulled out of the loop. Avoids unnecessary calculations associated with special iterations; also allows fusion of loops with slightly different iteration ranges



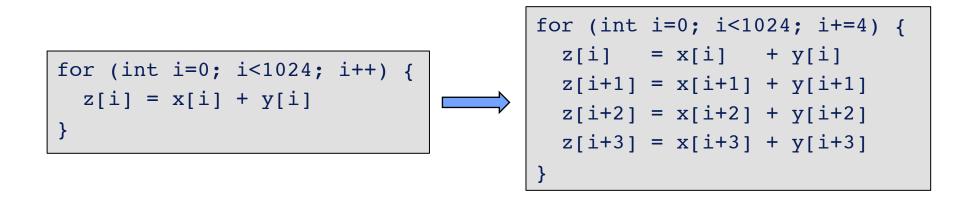
The example above illustrates how peeling off the first iteration of the first loop (i=0) both avoids special case (product instead of sum) and allows fusion with the following loop





Loop unrolling

Loop body is replicated and the stride is modified accordingly. This optimization can help the processor make better use of arithmetic functional units.



Note that this example is particularly simple since the loop count is divisible by the unrolling depth. In general, you'll need to write cleanup code to handle the leftover iterations (remainder of n/depth).

You will rarely beat the compiler and manual loop unrolling will make your code ugly and difficult to maintain. Best choice for unrolling depth may be processor architecture dependent.





Loop unrolling

Although you'll rarely beat the compiler, sometimes you'll encounter a loop that is too complex for it to accurately analyze. Below is an example where manual loop unrolling by 4x did better than the compiler (original loop shown)

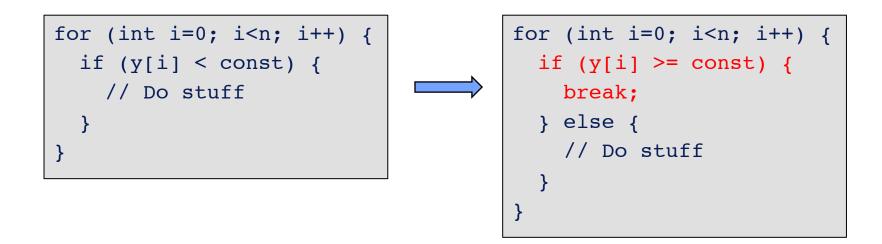
```
do i=0,4319,2 ! Unrolled loop → i=0,4319,8
  j0=mg63_miijj(0,i)
  j1=mg63_miijj(1,i)
  j2=mg63_miijj(2,i)
  i0=mg63_miijj(3,i)
  i1=mg63_miijj(4,i)
  i2=mg63_miijj(5,i)
  i3=mg63_miijj(6,i)
  pvi3jj(1) = pvi3jj(1) + d(i0,i1)*d(i0,i2)*d(i0,i3)*d(i0,j0)*d(i0,j1)
  pvi3jj(2) = pvi3jj(2) + d(i0,i1)*d(i1,i2)*d(i0,i3)*d(i0,j0)*d(i0,j1)
  pvi3jj(3) = pvi3jj(3) + d(i0,i1)*d(i1,i2)*d(i1,i3)*d(i0,j0)*d(i0,j1)
  ...
  pvi3jj(22) = pvi3jj(22) + d(i0,i2)*d(i0,i3)*d(i0,j0)*d(i1,j0)*d(j0,j1)
  pvi3jj(23) = pvi3jj(23) + d(i1,i2)*d(i0,i3)*d(i0,j0)*d(i1,j0)*d(j0,j1)
  pvi3jj(24) = pvi3jj(24) + d(i0,i2)*d(i2,i3)*d(i0,j0)*d(i1,j0)*d(j0,j1)
  enddo
```





Breaking out of loop early

Look for opportunities to break out of a loop early. This will generally require that you understand the semantics of your code



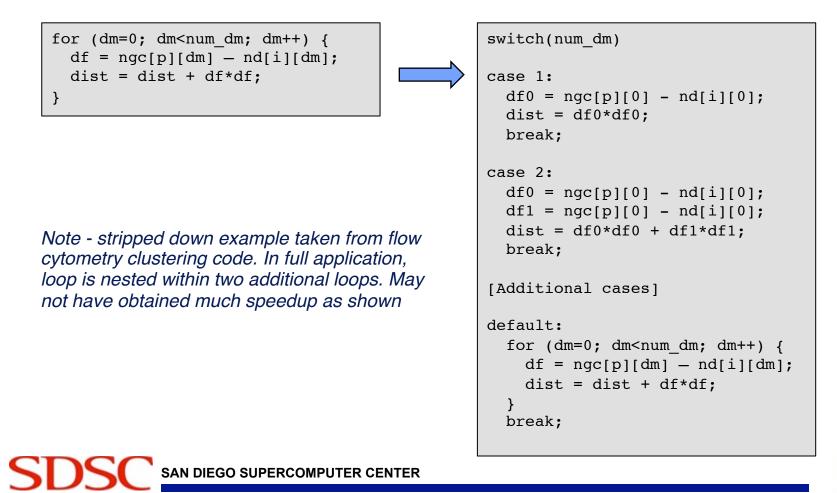
In this simple example (taken from real-life application), I used my knowledge that the elements of array y are monotonically increasing $(y[0] \le y[1] \le y[2] \le y[3] \dots$). The compiler only understands the syntax of your code and cannot safely do this optimization for you.





Short loop optimizations

If you expect that a loop body may be executed for a small number of iterations, can generate specific code for special cases.





Non cache/loop optimizations

- Although there is some overlap between loop and non-loop optimizations, these techniques are generally applied at the statement or whole program level.
- The compiler can do some of these for you (e.g. constant propagation). Others, such as force reduction and (especially) inter-procedural optimization will usually require that the programmer modify the code.
- Unless it makes your code excessively difficult to read or maintain, suggest that you do these yourself. Will avoid surprises when using different versions of compilers or optimization levels.





Obviousness alert!

Some of the things that I'll be discussing in this presentation are completely obvious. That said, they're still worth pointing out since they are often overlooked and only become obvious after the fact

Federal Agents Raid Gun Shop, Find Weapons Store Owner Arrested Previously On July 2, undercover mar-By Brian Barber cotics agents served a war World Staff Writer rant at Thao's t deral anents on Mond



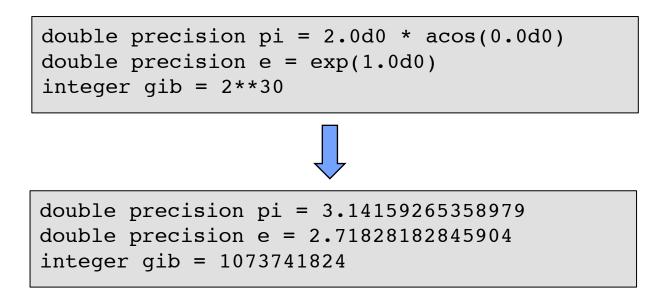




at the UNIVERSITY OF CALIFORNIA; SAN DIEGO

Constant folding

Compiler recognizes constant expressions and evaluates at compile time rather than performing operations at run time. These are trivial for the compiler and there's no reason to do them yourself, especially if the original code is easier to understand

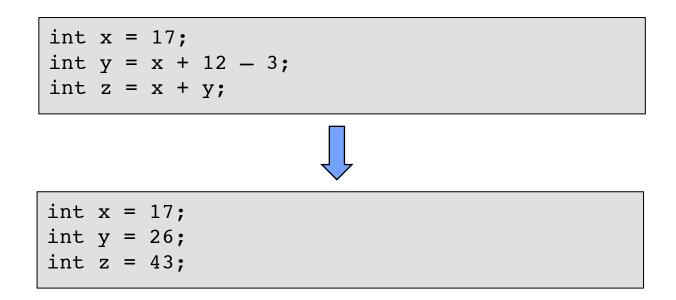






Constant propagation

Constants are propagated at run time into other expressions that depend on them. Trivial for the compiler to do these, no reason to implement manually if it makes code more difficult to read.

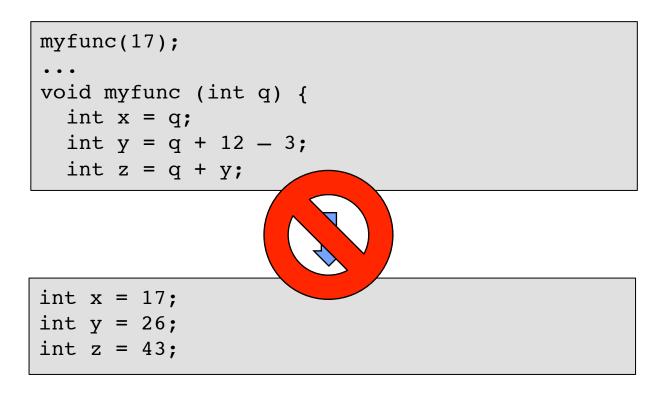






If the compiler does this, why are we even talking about it here?

Constant folding and propagation depend on the compiler having enough information to do the optimizations. If your program uses constants, be sure to code them explicitly.





Force reduction

A force reduction optimization involves the replacement of an expensive operation with a less expensive one.

Exponentiation operations, especially floating point base raised to a floating point power, are particular expensive. Look for opportunities to replace with multiplications, particularly if the exponent is known at compile time

pow(x,8.0) \rightarrow x2 = x*x; x4 = x2*x2; x8 = x4*x4 pow(x,1.5) \rightarrow y = x * sqrt(x)

Fortran and newer versions of C++ overload the pow() function. Use integer exponent whenever possible

double precision x,y \rightarrow double precision x x^{**}y integer n x^{**}n





Force reduction

Operations involving trig functions can often be simplified by using the trig identifies that you learned in high school. Just make sure that your transformation apply to all quadrants if applicable

 $sin(x)^*cos(x) \rightarrow 0.5^*sin(2^*x)$ $sin(x)^*cos(y)+cos(x)^*sin(y) \rightarrow sin(x+y)$

If a and b are fixed and sum needs to be calculated repeatedly for many values of x, can pre-calculate the constants c and phi.

 $a^*sin(x) + b^*cos(x)$ \rightarrow $c^*sin(x+phi)$ $c = sqrt(a^*a + b^*b)$ phi = atan2(b,a)

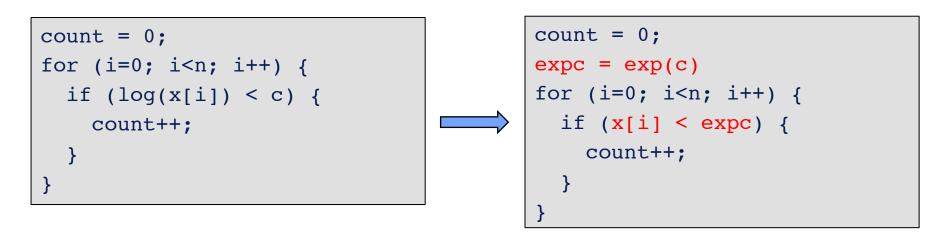


SAN DIEGO SUPERCOMPUTER CENTER

at the UNIVERSITY OF CALIFORNIA; SAN DIEGO

Force reduction

There are often hidden opportunities for force reductions. Look at logical tests that can be written in a more efficient way. Think about what results are really needed.



In this example, we didn't really need to know the logarithm of x[i] and we could recast using a simple comparison to a pre-computed value.





Force reduction exercise

- Copy the disttest.c file to your home directory. Program generates a set of randomly distributed points in the unit square and calculates number that are separated by less than a specified tolerance. Inspect the code and make sure you understand logic.
- Compile program using the following options

icc -O3 -o disttest disttest.c

 Run executables on Gordon compute node and keep track of run times as reported by code. Try n=10000, 50000, 100000 and various values for tolerance

./disttest 50000 0.01

• Apply force reduction optimization to reduce the run time





Short circuiting

Most imperative programming languages (MATLAB, Perl, Python, Java, Fortran, C/C++) use short circuit evaluation for compound logical tests

Disjunctions ('OR' tests) evaluate to TRUE once the first argument that evaluates to TRUE is encountered

Conjunctions ('AND' tests) evaluate to FALSE once the first argument that evaluates to FALSE is encountered

As a consequence, subsequent arguments are not evaluated once the final result is known. We can take advantage of this to write more efficient code.





Short circuiting (disjunction)

Some good rules of thumb for ordering arguments (P II Q)

1. If P and Q take roughly the same amount of time to evaluate, put the argument that is more commonly TRUE first

if (usually_true II usually_false) if (sin(x) > 0.01 II cos(y) < 0.01) // 0 ≤ x,y ≤ $\pi/2$ uniformly distributed

2. If P and Q are vastly different in the time required for evaluation, put the faster test first

if (fast_test II slow_test)
if (x > y II pow(x,y)/atan2(w,z) > log(sqrt(x/y))





Short circuiting (conjunction)

Some good rules of thumb for ordering arguments (P && Q)

1. If P and Q take roughly the same amount of time to evaluate, put the argument that is more commonly FALSE first

if (usually_false && usually_true) if (cos(y) < 0.01 && sin(x) > 0.01) // 0 \leq x,y \leq $\pi/2$ uniformly distributed

2. If P and Q are vastly different in the time required for evaluation, put the faster test first

if (fast_test && slow_test) if (x > y & pow(x,y)/atan2(w,z) > log(sqrt(x/y))





Avoid recalculating results

One of the easiest ways to reduce runtime is to avoid calculating a result multiple times. Sometimes the compiler can recognize this and pre-calculate the result

<u>Original</u>	Compiler will probably do this
$a = w + x^*x + sqrt(y)$	$temp = x^*x + sqrt(y)$
$b = z + x^*x + sqrt(y)$	a = w + temp
	b = z + temp

For user defined function, compiler needs to be careful of side effects and may not be able to safely perform the optimization $a = w + x^*x + myfunc(y)$ // Did myfunc change a global variable? $b = z + x^*x + myfunc(y)$ // Will the 2nd call return the same result?





Avoid recalculating results (cont.)

Pre-calculating results can have an even bigger impact when the result is calculated repeatedly in a loop body. This is know as a loop invariant optimization

```
for (i=0; i<n; i++) {
    a[i] = b[i] + sqrt(c);
}</pre>
```

The compiler will generally recognize simple invariants and pull outside of the loop. For the above example, the compiler will generate code like the following



Inter-procedural optimizations

- Until now, we've mostly been focusing on optimizations at the loop or function level. More difficult are inter-procedural optimizations, which require considering the application as a whole
- Compilers are great at optimizing loops (inversion, unrolling, fusion, splitting, peeling ,etc.) and statements, but can rarely recognize opportunities for inter-procedural optimizations.
- These generally require an intimate understanding of your code.
- Very often, this optimization requires that you recognize operations that are repeated on the same set of data from one invocation of a function to the next.





Inter-procedural optimization (example 1)

In a flow-cytometry code, noticed that a function was called five times in a row with slightly different sets of arguments (diffs highlighted in red)

```
Ei=get_avg_dist(rpc[temp_i], temp_i, temp_j, population_ID,
num_real_pop, file_Len, num_dm, norm_data, d1, d2, d3, size_c);
Ej=get_avg_dist(rpc[temp_j], temp_i, temp_j, population_ID,
num_real_pop, file_Len, num_dm, norm_data, d1, d2, d3, size_c);
E1=get_avg_dist(center_1, temp_i, temp_j, population_ID,
num_real_pop, file_Len, num_dm, norm_data, d1, d2, d3, size_c);
E2=get_avg_dist(center_2, temp_i, temp_j, population_ID,
num_real_pop, file_Len, num_dm, norm_data, d1, d2, d3, size_c);
E3=get_avg_dist(center_3, temp_i, temp_j, population_ID,
num_real_pop, file_Len, num_dm, norm_data, d1, d2, d3, size_c);
```





Inter-procedural optimization (example 1)

Within the get_avg_dist function, the key loops involve a comparison between elements of population_ID and the scalars (temp_i, temp_j) to decide which elements of norm_data are used for the calculations. Recall that center is the only argument to change between calls and the same elements of norm_data are used all five times

```
get_avg_dist(center, temp_i, temp_j, population_ID,
num_real_pop, file_Len, num_dm, norm_data, d1, d2, d3, size_c);
```

```
for (i=0; i<file_Len; i++) {
    if (population_ID[i]==temp_i || population_ID[i] ==temp_j) {
      dist1 = center[d1] - norm_data[i][d1];
      dist2 = center[d2] - norm_data[i][d2];
      dist3 = center[d3] - norm_data[i][d3];
      d = dist1*dist1 + dist2*dist2 + dist3*dist3;
      if (d < radius) num_neighbors++
}</pre>
```



Inter-procedural optimization (example 1)

To avoid having to do the same tests five times in a row, do a "gather" operation to collect elements of packed data into an array and pass as argument to a modified get_avg_dist. Led to ~ 3x speedup of program.

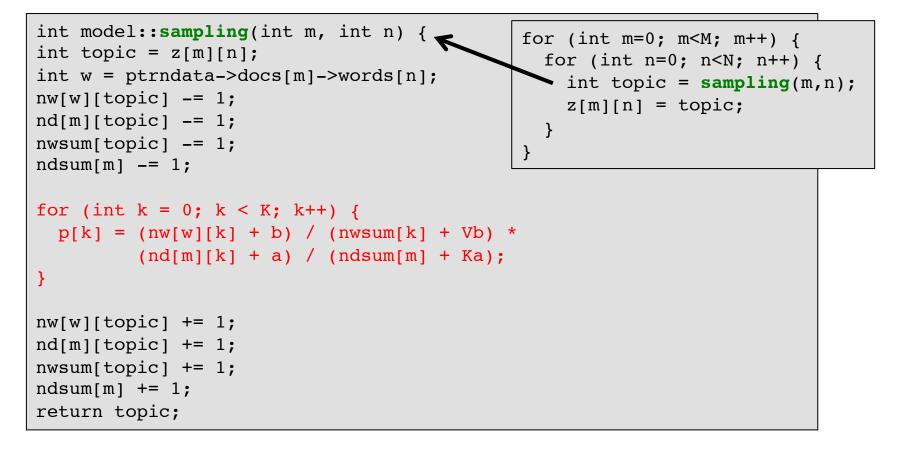
```
npacked = 0;
for (i=0;i<file_Len;i++) {
    if (population_ID[i]==temp_i || population_ID[i]==temp_j){
        packed1[npacked] = norm_data[i][d1];
        packed2[npacked] = norm_data[i][d2];
        packed3[npacked] = norm_data[i][d3];
        npacked++;
    }
}
```

```
for (i=0; i<npacked; i++) {
   dist1 = center[d1] - packed1[i];
   dist2 = center[d2] - packed2[i];
   dist3 = center[d3] - packed3[i];
   d = dist1*dist1 + dist2*dist2 + dist3*dist3;
   if (d < radius) num_neighbors++
}</pre>
```



Inter-procedural optimization (example 2)

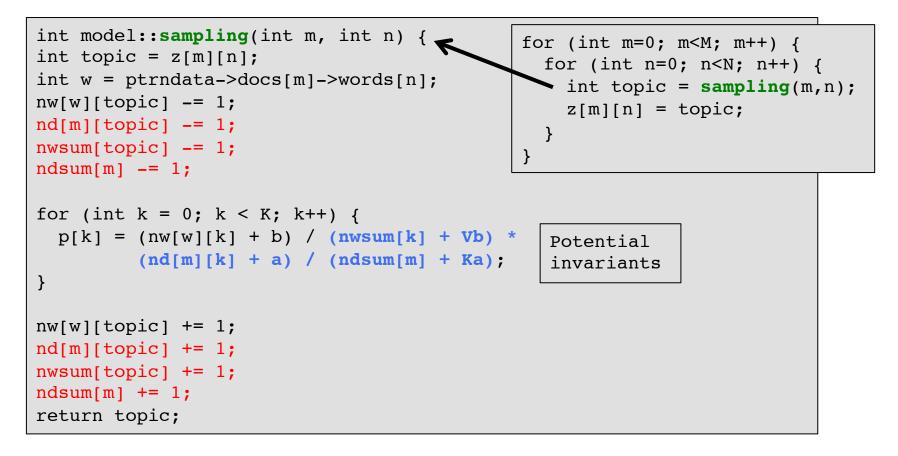
In Latent Dirichlet Allocation code (identifies topics in free text), profiling shows that nearly all time spent in a single method





Inter-procedural optimization (example 2)

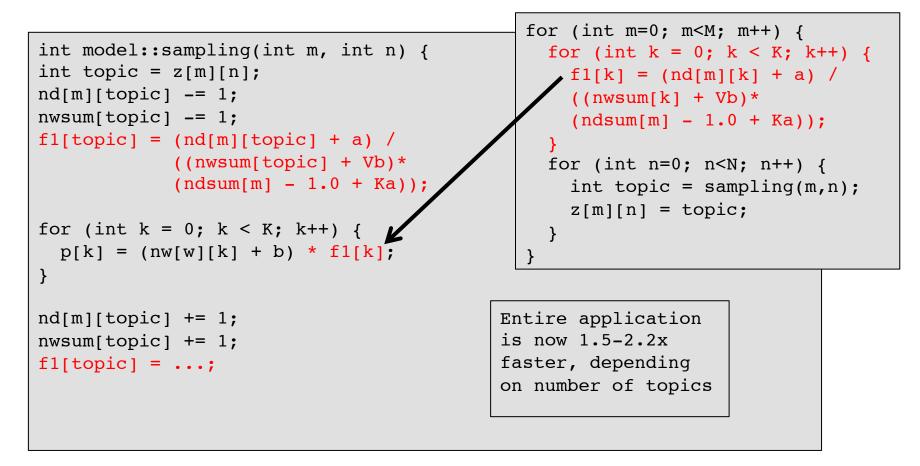
Note that sampling(m,n) called repeatedly with same value of m and that only a few elements of nd, nwsum and ndsum are (temporarily) updated





Inter-procedural optimization (example 2)

Pre-calculate array of values that do not change (much) across successive calls to sampling and update only necessary elements





Unique optimizations

- Standard techniques will take you a long way, but sometimes you get the biggest payoffs from novel, one-off optimizations
- These are also the most fun optimizations. To me, it's like getting paid to do brain ticklers
- Often requires a more intimate understanding of your application
- Once you've identified your hotspot, single-mindedly focus your efforts on a better, faster solution
- Hard to provide concrete advice since the specific optimization tends to be very problem specific. Here's the best I can do:
 - Be smart
 - Even better, be clever
 - Be obsessive
 - Revisit your high school algebra, trig and geometry





Approximate expensive function and redo accurate calculation only when necessary

Fortran application was spending most of its time calculating inverse cosine (acos) function. Result used in test that is rarely satisfied

```
if (acos(xprod) < abs(xi-xj)) then
    -- do some calculations --
endif</pre>
```

Google search found an inexpensive approximation (20x faster) to inverse cosine ($\pi/2$ - Ax⁵ - Bx) with a known maximum error. Use for initial test and recalculate acos only when needed. Note that this has no impact on final results

```
if(acos_approx(xprod) < abs(xi-xj) + max_err) then
    if(acos(xprod) < abs(xi-xj) then
        -- do some calculations --
    endif
endif</pre>
```



Fast calculation of sum over logs

Many problems in bioinformatics, statistical physics and other fields require the calculation of log probabilities. The direct product over small probabilities results in underflow, so we need to calculate sum over logs instead

Want
$$\log(\prod_{i=1}^{n} p_i)$$
, but $\prod_{i=1}^{n} p_i$ underflows
Instead, calculate $\sum_{i=1}^{n} \log(p_i)$

The downside is that the latter is n times more expensive. This can have a big impact on performance if n is large and/or log probabilities are frequently calculated





Fast calculation of sum over logs (cont.)

To avoid the expensive logarithm calculations, first split arguments into normalized fractions $(1/2 \le x < 1)$ and powers of two. Can do this with the very fast C frexp function. Then accumulate product over fractions, sum over powers of two and do a little algebra at the end

 $5 \times 17 \times 37 = (0.625 \times 2^3) \times (0.53125 \times 2^5) \times (0.578125 \times 2^6)$ = (0.625 x 0.53125 x 0.578125) x 2¹⁴ = 0.1919556 x 2¹⁴ $\log(5 \times 17 \times 37) = \log(0.1919556) + \log(2.0) \times 14 = 3.49762 \checkmark$



SAN DIEGO SUPERCOMPUTER CENTER

at the UNIVERSITY OF CALIFORNIA; SAN DIEGO

Fast calculation of sum over logs (cont.)

What if the product over fractions underflows? Multiply by constant to keep product close to one and correct for this later. Assumes that the fractional parts of the arguments are uniformly distributed between ½ and 1. Here's the final solution

```
c=1.358858;
sprod = 1.0;
xsum = 0.0;
for (i=0; i<n; i++) {
   s = frexp(p[i], &x); // Split into fraction and power of 2
   sprod *= (s * c); // Product over fractions, with correction
   xsum += x; // Sum over powers of two
}
logsum = log(sprod) + log(2.0)*xsum - n*log(c);
```



log sum exercise

- Copy the logsum.c file to your home directory. Program performs log sum using both standard and optimized method. Inspect the code and make sure you understand logic.
- Compile program using the following options

gcc -O3 -o logsum_gcc logsum.c -Im icc -O3 -o logsum_icc logsum.c

- Run executables on Gordon compute node and keep track of run times as reported by code. Try altering the following (line 15), but keeping n*m constant
 - n (number of contributions to log sum)
 - m (number of trials)





log sum exercise

- Are there any noticeable differences between the timings for the Intel (icc) and GNU (gcc) compilers?
- Did you notice any trends in the ratio of run times as a function of problem size?
- If you noticed a difference between the compilers why do you think this happened?





Linear algebra - DSYRK

After initial rounds of optimization, determined that application was spending most of its time in the DSYRK linear algebra routine

 $D \leftarrow \alpha AA^T + \beta D$ (A and C matrices, α and β and constants)

Figured that there was no room left for improvement, then took a more careful look at the way the matrix A is constructed from the concatenation of two matrices

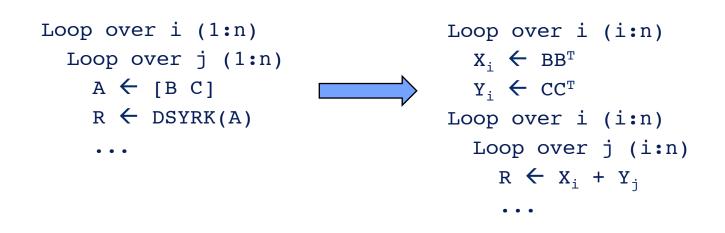
$$\begin{array}{l} \begin{array}{c} Rewrite \ A \ as \\ concatenation \ of \\ two \ matrices \ A \\ and \ B \end{array} \qquad \begin{bmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{bmatrix} = \begin{bmatrix} b_{11} & b_{12} & c_{11} & c_{12} \\ b_{21} & b_{22} & c_{21} & c_{22} \\ b_{31} & b_{32} & c_{31} & c_{32} \\ b_{41} & b_{42} & c_{41} & c_{42} \end{bmatrix} = \begin{bmatrix} B & C \end{bmatrix} \begin{bmatrix} B & C \end{bmatrix}$$

$$\begin{array}{c} AA^{T} \ can \ be \\ expressed \ as \\ BB^{T} \ + \ CC^{T} \end{array} \qquad AA^{T} = \begin{bmatrix} B & C \end{bmatrix} \begin{bmatrix} B & C \end{bmatrix} \begin{bmatrix} B & C \end{bmatrix}^{T} = \begin{bmatrix} B & C \end{bmatrix} \begin{bmatrix} B^{T} \\ C^{T} \end{bmatrix} = BB^{T} \ + \ CC^{T} \end{array}$$



Linear algebra - DSYRK (cont.)

Further inspection revealed that the nested loops over indices provides opportunities for pre-calculating the partial results (BB^T, CC^T) and replacing the DSYRK call with a much faster matrix addition.







A few words about optimizing parallel codes

- Fast parallel codes depend on fast underlying serial algorithms
- We don't have time to get into optimization of parallel algorithms, but here are a few things to consider
- Address load balancing make sure that each process or thread is assigned the same amount of work (or at least as close as possible)
- Minimize communications overhead
 - Try to overlap communication and computation
 - Avoid unnecessary serialization or synchronization events
 - Send fewer large message rather than more small messages





Load balancing in OpenMP code

If all iterations take the same amount of time, static decomposition is fine. Otherwise, consider dynamic assignment of work.

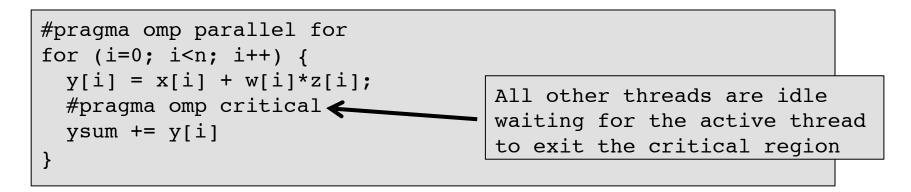
```
#pragma omp parallel for
for (i=0; i<n; i++) {
    // All iterations take same amount of time
}
#pragma omp parallel for schedule(dynamic,n)
for (i=0; i<n; i++) {
    // Iterations take different times
    // May need to experiment with "n"
    // Use n=1 if orders of magnitude variation in run time
}
```

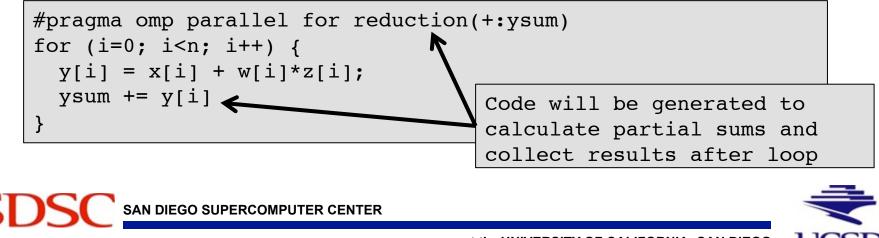




Avoid serialization in OpenMP code

Look for ways to avoid synchronization events in loops. Consider reduction variables or restructuring of logic





Avoid synchronization in MPI code

Think about whether or not synchronization is really needed

